Math 6327 Real Analysis

1. Let A be a measurable set of real numbers with the property that

$$(x, y \in A \text{ and } x \neq y) \Longrightarrow (x+y)/2 \notin A.$$

Show that A has measure zero.