## Assignment 2 Math 2413

## August 20, 2008

- 1. Read bogus  $\S2.1$ .
- 2. Look at the bogus problems 2.1.1, 3,6,7,10,12,17,18,22,26,35.
- 3. Let  $f: [0,1] \to \mathbb{R}$  be a continuous function such that  $\int_0^1 f(t)\eta(t)dt = 0$  for all  $\eta \in C_c^{\infty}[0,1]$ . What can you say about f?

Notes:

- (a) Here we could simply write  $f \in C^0[0, 1]$ .
- (b)  $C^{\infty}$  denotes the functions which have derivatives of all orders, both existing and continuous.
- (c)  $C_c^{\infty}$  denotes the subspace of  $C^{\infty}$  of the functions with *compact support*. The *support* of a function is the closure of the set of all points at which the function is non-zero. To be *compactly supported* means that the support of the function is compact (i.e., closed and bounded) and is also a subset of the interior of the domain of the function. In this case, it means that  $\operatorname{supp}(f) \subset (0, 1)$ . In this case, we write  $\operatorname{supp}(f) \subset [0, 1]$ .
- 4. Find a nonzero function in  $C_c^{\infty}[0, 1]$ .
- 5. Vocabulary: differentiation under the integral sign, fundamental lemma (of the calculus of variations),  $C^k$ ,  $C^{\infty}$ ,  $C_c^{\infty}$ , compact support, closure, closed/open (sets), continuously differentiable ( $C^1$ ), compactly contained ( $\subset \subset$ ), continuity (review), numerical solution, tangent line (review), slope (review), slope field, difference quotient (review), limit

(review), piecewise linear, step size, Euler's method, round off error, Runge-Kutta method (will understand more fully later).